

Concept Question 6-7: How does one determine the length $N + 1$ of the PSF for motion blur from the spectrum of the blurred image?

The PSF, hence the DSFT of the blurred image, is zero when $\Omega(N + 1)/2$ is an integer multiple of π . See Eqs. (6.49) and (6.47) below.

$$\begin{aligned}
 \mathbf{H}(\Omega_1, \Omega_2) &= \text{DSFT}\{h[n, m]\} \\
 &= \text{DTFT}_{n \rightarrow \Omega_1} \left\{ \text{rect} \left[\frac{n - N/2}{N/2} \right] \right\} \\
 &\quad \times \text{DTFT}_{m \rightarrow \Omega_2} \{ \delta[m] \} \frac{T}{N} \\
 &= \frac{T}{N} \frac{\sin \left[\Omega_1 \left(\frac{N+1}{2} \right) \right]}{\sin(\Omega_1/2)} e^{-j\Omega_1 N/2}. \quad (6.49)
 \end{aligned}$$

$$h[n, m] = \text{rect} \left[\frac{n - N/2}{N/2} \right] \delta[m] \Delta_t. \quad (6.47)$$